## The University of Texas at Austin Dept. of Electrical and Computer Engineering Midterm #2

Date: November 16, 2021

Course: EE 313 Evans

Name:

Last,

First

- This in-person exam is scheduled to last 75 minutes.
- Open books, open notes, and open class materials, including homework assignments and solution sets and previous midterm exams and solutions.
- Calculators are allowed.
- You may use any standalone computer system, i.e. one that is not connected to a network.
- Please disable all wireless connections on your calculator(s) and computer system(s).
- Please mute all computer systems.
- Please turn off all phones.
- No headphones are allowed.
- All work should be performed on the midterm exam. If more space is needed, then use the backs of the pages.
- <u>Fully justify your answers</u>. If you decide to quote text from a source, please give the quote, page number and source citation.

Problem	Point Value	Your score	Topic	
1	27		System Properties	
2	27		Convolution	
3	26		Highpass Filters	
4	20		Wireless Localization	
Total	100			

## Problem 2.1. System Properties. 27 points.

Each discrete-time system has input x[n] and output y[n], and x[n] and y[n] might be complex-valued. Each continuous-time system has input x(t) and output y(t), and x(t) and y(t) might be complex-valued. Determine if each system is linear or nonlinear, time-invariant or time-varying, and stable or unstable.

You must either prove that the system property holds in the case of linearity, time-invariance, or stability, or provide a counter-example that the property does not hold. Providing an answer without any justification will earn 0 points.

Part	System Name	System Formula	Linear?	Time- Invariant?	Stable?
(a)	Averaging Filter	y[n] = x[n] + x[n-1] for $n \ge 0$ and $x[-1] = 0$			
(b)	Frequency modulation	$y(t) = \cos\left(2\pi f_c t + 2\pi k_f \int_0^t x(\lambda) d\lambda\right)$			
		for $t \ge 0$ . $f_c$ and $k_f$ are real-valued constants.			
(c)	Time Reversal	$y(t) = x(-t)$ for $-\infty < t < \infty$			

(a) Averaging filter: y[n] = x[n] + x[n-1] for  $n \ge 0$  and x[-1] = 0. 9 points.

(b) Frequency Modulation:  $y(t) = \cos\left(2\pi f_c t + 2\pi k_f \int_0^t x(\lambda) d\lambda\right)$  for  $t \ge 0$ . 9 points.

(c) Time reversal: y(t) = x(-t) for  $-\infty < t < \infty$ . 9 points.

## Problem 2.2 Convolution. 27 points.

In continuous-time systems, an linear time-invariant (LTI) integrator is a building block. Its inputoutput relationship is

$$y(t) = \int_{-\infty}^{t} x(\tau) \, d\tau$$

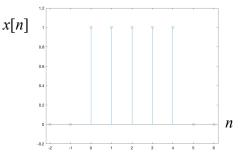
The impulse response is h(t) = u(t) where u(t) is 1 for  $t \ge 0$  and 0 otherwise.

The equivalent system in discrete time is the LTI running summation system. Its input-output relationship is

$$y[n] = \sum_{m=-\infty}^{n} x[m]$$

The impulse response is h[n] = u[n] where u[n] is 1 for  $n \ge 0$  and 0 otherwise.

(a) Plot the output y[n] of the LTI running summation when the input is a five-point rectangular pulse  $x[n] = \delta[n] + \delta[n-1] + \delta[n-2] + \delta[n-3] + \delta[n-4]$ ? On the right, x[n] is plotted for  $-2 \le n \le 6$ . 9 points.



(b) Give a formula for the output y[n] of the LTI running summation when the input is x[n] = u[n]. The formula should be valid for  $-\infty < n < \infty$ . 9 points.

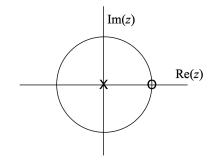
(c) Give a formula for the output y(t) of the LTI integrator when the input is x(t) = u(t). The formula should be valid for  $-\infty < t < \infty$ . 9 points.

Problem 2.3. Highpass Filters. 26 points.

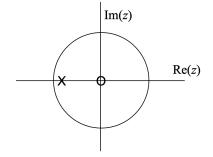
A highpass filter passes high frequencies and attenuates low frequencies.

Shown below are the pole-zero plots for two discrete-time linear time-invariant (LTI) highpass filters.

- (a) LTI first-order finite impulse response (FIR) filter. Pole-zero plot on the right. Zero at z = 1 and pole at z = 0.
  - i. Write the transfer function H(z) including the region of convergence. 6 points.



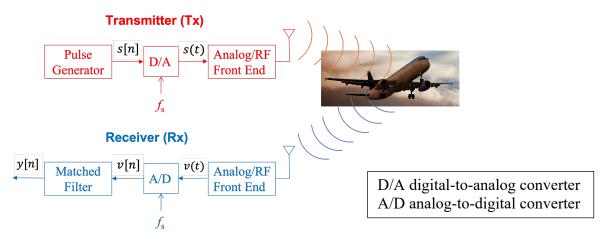
- ii. Give a formula for the frequency response. *3 points*.
- iii. Plot the magnitude response. 4 points.
- (b) LTI first-order infinite impulse response (IIR) filter. Pole-zero plot on the right. Pole at z = -0.9 and zero at z = 0.
  - i. Write the transfer function H(z) including the region of convergence. 6 points.
  - ii. Give a formula for the frequency response. *3 points*.
  - iii. Plot the magnitude response. 4 points.



## Problem 2.4 Wireless Localization. 20 points.

Mini-Project #2 used radar (electromagnetic waves and signal processing) to locate an object in an environment. Applications include automotive and 6G cellular communication systems.

A block diagram for the radar system to determine the distance to the object follows.



The radar system estimates the round-trip time  $T_d$  from the transmitter to the object and from the object to the receiver. Transmitter and receiver are in the same location. Distance *d* can be computed using  $d = \frac{1}{2} c T_d$  where *c* is the speed of propagation of electromagnetic waves in air (speed of light).

(a) What are the advantages of using a chirp pulse for the transmitted waveform? 6 points.

(b) Describe the role of the matched filter in the receiver. Why is it called a matched filter? What is being matched? *6 points*.

(c) How did the radar system use the chirp pulse and matched filter to estimate the round-trip time  $T_d$  from the transmitter to the object and from the object to the receiver? 8 points.